An opera company selects from among six operas— Fidelio, La Boheme, Otello, Siegfried, Tosca and Zauberflöte—to perform during a given opera season. Each opera, if performed, will be performed exactly once. The list of operas performed is consistent with the following conditions:

 $\label{eq:continuous} \text{If } \textit{Tosca} \text{ is performed, then } \textit{Zauberfl\"ote} \text{ is } \\ \text{not.}$

Fidelio is performed only if *Tosca* is performed.

If *La Boheme* is performed, then so is *Zauberflöte*.

If *Fidelio* is not performed, then *Siegfried* is. If *Tosca* is not performed, *Otello* is not performed.

- 1. Which one of the following could be a complete and accurate list of the operas performed in a given season?
- A. Fidelio, La Boheme, Otello, Siegfried
- B. La Boheme, Otello, Tosca, Zauberflöte
- C. Fidelio, La Boheme, Tosca, Zauberflöte
- D. La Boheme, Siegfried, Tosca
- E. Fidelio, Tosca
- 2. If *Fidelio* is not performed in a given opera season, then each of the following could be true about that opera season EXCEPT
- A. Tosca is performed.
- B. Otello is performed.
- C. Neither *La Boheme* nor *Tosca* is performed.
- D. Neither *La Boheme* nor *Siegfried* is performed.
- E. Neither *Otello* nor *Tosca* is performed.

- 3. If in a given opera season both *Otello* and *Tosca* are performed, then which one of the following must be true in that opera season?
- A. *La Boheme* is the only other opera performed.
- B. Siegfried is the only other opera performed.
- C. At most two other operas are performed.
- D. Neither Fidelio nor Siegfried is performed.
- E. Exactly one other opera is performed.
- 4. If *Zauberflöte* is performed in a given opera season, then which one of the following must be true during that opera season?
- A. Siegfried is performed.
- B. La Boheme is performed.
- C. Both *La Boheme* and *Siegfried* are performed.
- D. At most one other opera is performed.
- E. At least two other operas are performed.
- 5. Which one of the following is the maximum number of operas which could be performed during a given opera season?
- A. two
- B. three
- C. four
- D. five
- E. six
- 6. Each of the following is a pair of operas which could be performed together EXCEPT
- A. Fidelio, Otello
- B. Fidelio, La Boheme
- C. Fidelio, Siegfried
- D. Siegfried, La Boheme
- E. Siegfried, Otello

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- 1. E
- 2. D
- 3. C
- 4. A
- 5. C
- 6. B

Question 1, like most first questions, is a testing of the rules. All four answer choices violate one of the conditions. Question 2 is D because if *Fidelio* is performed, *Siegfried* must be performed. On Question 3, because *Tosca* can't be with *Zauberflöte* and because *La Boheme* means the existence of *Zauberflöte*, then *Tosca* can't be with either of those—and thus only two more operas can be performed.

On Question 4, the key is that you need either *Fidelio* or *Siegfried* under the rules, and you can't have *Fidelio* if *Zauberflöte* is performed. For the maximum number question, remember to identify rules that require two things to not be together. There is only one such rule—the *Tosca* and *Zauberflöte* rule—but *La Boheme* impels the existence of *Zauberflöte* and thus cannot be included in such a maximum list as well. On Question 6, you cannot have both *Fidelio* and *La Boheme* because *Fidelio* means *Tosca* and *La Boheme* means *Zauberflöte*, and *Tosca* and *Zauberflöte* can't go together.